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# Searching for similar trajectories in spatial networks

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#### ABSTRACT

In several applications, data objects move on pre-defined spatial networks such as road segments, rail-ways, and invisible air routes. Many of these objects exhibit similarity with respect to their traversed paths, and therefore two objects can be correlated based on their motion similarity. Useful information can be retrieved from these correlations and this knowledge can be used to define similarity classes. In this paper, we study similarity search for moving object trajectories in spatial networks. The problem poses some important challenges, since it is quite different from the case where objects are allowed to move freely in any direction without motion restrictions. New similarity measures should be employed to express similarity between two trajectories that do not necessarily share any common sub-path. We define new similarity measures based on spatial and temporal characteristics of trajectories, such that the notion of similarity in space and time is well expressed, and moreover they satisfy the metric properties. In addition, we demonstrate that similarity range queries in trajectories are efficiently supported by utilizing metric-based access methods, such as M-trees.

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#### 1. Introduction

In location-based services it is important to query the underlying objects based on their location in space, which may change with respect to time. To support such services from the database point of view, specialized tools are required which enable the effective and efficient processing of queries. Queries may involve the spatial or temporal characteristics of the objects, or both (spatio-temporal queries) (Wolfson et al., 1998; Theodoridis et al., 1998). Evidently, indexing schemes are ubiquitous to efficiently support queries on moving objects, by quickly discarding non-relevant parts of the database.

We distinguish between two different research directions towards query processing in moving objects, which differ both in the type of queries supported and the characteristics of the indexing schemes used in each case:

[I] Query processing techniques for past positions of objects, where past positions of moving objects are archived and queried, using multi-version access methods or specialized access methods for object trajectories (Lomet and Salsberg,

1989; Nascimento and Silva, 1998; Pfoser et al., 2000; Tao and Papadias, 2001a,b). By studying the past positions of objects, important conclusions can be obtained regarding their mobility characteristics. The difficulty in this case is that the database volume increases considerably, since new positions are tracked and recorded.

[II] Query processing techniques for present and future positions of objects, where each moving object is represented as a function of time, giving the ability to determine its future positions according to the current motion characteristics of objects (reference position, velocity vector) (Kollios et al., 1999a,b; Wolfson et al., 2000; Saltenis et al., 2000; Lazaridis et al., 2002). These methods are mainly used to support queries according to the current positions and enable predictions of their future locations. The difficulty in this case is to perform effective predictions, which is difficult taking into consideration that some positions will be invalidated, due to changes in the speed and direction of some objects in the near future.

A data set of moving objects is composed of objects whose positions change with respect to time (e.g., moving vehicles). Since in many cases only the position of each object is important, moving objects are modeled as *moving points* in 2D or 3D Euclidean space. Queries that involve a particular time instance are characterized as *time-slice queries*, whereas queries that must be evaluated for an interval  $[t_s, t_e]$  are characterized as *time interval queries*. The

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research community has studied both types extensively. Examples of basic queries that could be posed to such a data set include:

- Window query: given a rectangle R, which may change position and size with respect to time, determine the objects that are covered by R from time point t<sub>s</sub> to t<sub>e</sub>.
- Nearest-neighbor query: given a moving point P determine the k nearest-neighbors of P within the time interval  $[t_s, t_e]$ .
- Join query: given two moving data sets U and V, determine the pairs of objects  $(o_1, o_2)$  with  $o_1 \in U$  and  $o_2 \in V$  such that  $o_1$  and  $o_2$  overlap at some point in  $[t_s, t_e]$ .

Apart from the query processing techniques proposed for the fundamental types of queries (i.e., window, *k*-NN and join), the issue of *trajectory similarity* has been studied recently. The problem is to identify similar trajectories with respect to a given query trajectory.

The common characteristic of the aforementioned approaches and research works is that objects are allowed to move freely in 2D or 3D space, without any motion restrictions. However, in a large number of applications, objects are allowed to move only on pre-defined paths of an underlying network, resulting in constraint motion. For example, vehicles in a city can only move on road segments. In such a case, the Euclidean distance between two moving objects does not reflect their real distance. Fig. 1 shows such an example which illustrates the differences between restricted and unrestricted trajectories. Objects moving in a spatial network follow specific paths determined by the graph topology, and therefore arbitrary motion is prohibited. This means that two trajectories which are similar regarding the Euclidean distance may be dissimilar when the network distance is considered. The majority of existing methods for trajectory similarity assume that objects can move anywhere in the underlying space, and therefore do not support motion constraints. Most of the proposals are inspired by the time series case, and provide translation invariance, which is not always meaningful in the case of spatial networks. To attack this problem, the network is modeled as a directed graph, and the distance between two objects is evaluated by using algorithms for shortest paths between the nodes of the graph.

Therefore, the challenge is to express trajectory similarity by respecting network constraints, which is also a strong motivation for the following real and practical applications:

- [I] By identifying similar trajectories, effective data mining techniques (e.g., clustering) can be applied to discover useful patterns. For example, a dense cluster is an indication of emerge traffic measures, future road expansions, trafficjam detection, traffic predictions, etc.
- [II] Trajectory similarity can also help in several road network applications such as, routing applications which support historical trajectories, logistic applications, city emergency handling, drive guiding systems, flow analysis, etc. In such applications, efficient indexing and query processing techniques are required.
- [III] Trajectory similarity of moving objects resembles path similarity of user click-streams in the area of web usage mining. By analyzing the URL path of each user, we are able to determine paths that are very similar, and therefore effective caching strategies can be applied. In web usage mining, web pages and URL links are modeled as a graph. A node in the graph represents a web page, and an edge from one page to another represents an existing link between them. The time spent by each user to a page is also recorded, and it is used in expressing path similarity, in addition to the number of common web pages along each path. In the existing approaches, two paths are considered similar only if they share at least one common web page, or if the paths contain web pages with similar concept. In trajectory similarity on the other hand, two trajectories may be characterized similar even if they do not share any nodes. Therefore, the existing web usage mining techniques are not directly applicable, and the detection of network trajectory similarities can accelerate the web usage mining queries.

The rest of the article is organized as follows. In the next section, we give the appropriate background, we present related work. In Section 3, trajectory similarity search is presented by investigating effective similarity measures between trajectories in a spatial network. Indexing and query processing issues are covered in Section 4, whereas Section 5 offers experimental results. Finally, Section 6 concludes the work.

#### 2. Related work

In several applications, the mobility of objects is constrained by an underlying spatial network. This means that objects cannot

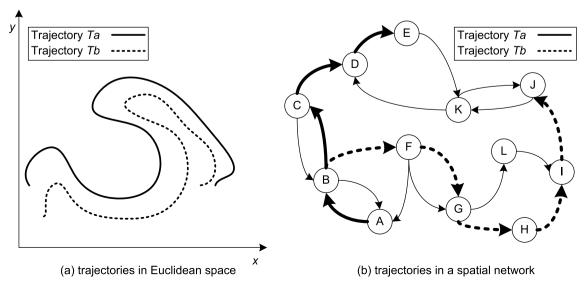


Fig. 1. Trajectories in (a) 2D Euclidean space, and (b) in a spatial network.

move freely, and their position must satisfy the network constraints. Network connectivity is usually modeled by using a graph representation, composed of a set of vertices (nodes) and a set of edges (connections). Depending on the application, the graph may be *weighted* (a cost is assigned to each edge) and *directed* (each edge has an orientation). Fig. 2 illustrates an example of a spatial network corresponding to a part of a city road network, and its graph representation.

Several research efforts have been performed towards efficient spatial and spatio-temporal query processing in spatial networks. In Sankaranarayanan et al. (2005) nearest-neighbor query processing is achieved by using a mapping technique. This mapping transforms the graph representation of the network to a highdimensional space, where Minkowski metrics can be used. Nearest-neighbor queries in road networks have been also studied in Iensen et al. (2003), where a graph representation is used to model the network. In Papadias et al. (2003) authors study query processing for stationary data sets, by using both a graph representation for the network and a spatial access method. It is shown that the use of Euclidean distance retrieves many candidates, and instead they propose a network expansion method to process range, nearest-neighbor and join queries. In-route nearest-neighbor queries have been studied in Yoo and Shekhar (2005), where given a trajectory source and destination the smallest detour is calculated.

The above contributions deal with efficient spatial or spatiotemporal query processing of fundamental queries like range, nearest-neighbor and join. However, the issue of trajectory similarity has not yet been studied adequately in the case of moving objects in spatial networks. Let  $T_a$  and  $T_b$  be the trajectories of moving objects  $o_a$  and  $o_b$ , respectively, and  $D(T_a, T_b)$  a function that expresses their dissimilarity in the range [0,1]. If the two objects have similar trajectories we expect the value  $D(T_a, T_b)$  to be close to zero. On the other hand, if the two trajectories are completely dissimilar, we expect the value  $D(T_a, T_b)$  to be close to one.

An example is illustrated in Fig. 3, where four trajectories are depicted in the 2D Euclidean space. A circle denotes the position of each moving object at the corresponding time instance  $(t_1,\ldots,t_8)$ . It is evident that one expects that the two gray-colored trajectories be very similar, in contrast to the two black-colored trajectories.

In several research proposals, trajectory similarity is viewed as the multidimensional counterpart of time series similarity. In Lee et al. (2000), the authors study the problem of similarity search in multidimensional data sequences, to determine similarities in image and video databases. A similarity model based on the Minkowski distance is defined, and each sequence is partitioned to subsequences by means of MBRs, to enable efficient indexing. This work can be viewed as an extension of the method proposed in Faloutsos et al. (1994) for time series data.

In Yanagisawa et al. (2003) a similarity distance between trajectories is defined, which is invariant to translation, rotation and

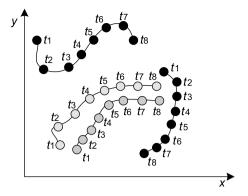


Fig. 3. Example of four trajectories in the 2D Euclidean space.

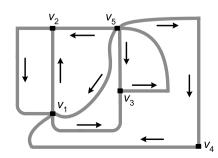
scaling. Again, the distance calculation is based on the Minkowski distance. Objects are allowed to move freely in the address space.

In Meratnia and de By (2002), an approach is studied to aggregate similar trajectories using a grid-based spatial unit aggregation. The notion of spatial similarity lies on the neighboring cells of the grid in a standard two-dimensional Euclidean space. Many problems can be arisen with how the grid must be defined, what the cell dimensions must be, and in objects and clusters identification.

In Laurinen et al. (2006), an efficient algorithm for trajectories similarity calculation is presented. But all distance calculations through trajectories are based on Euclidean metrics and spaces ( $L_p$  norms).

The method proposed in Vlachos et al. (2002a,b) employs a similarity distance based on the longest common subsequence (LCS) between two trajectories. This approach proposes a distance measure, which is more immune to noise than the Minkowski distance, but does not satisfy the metric space properties, and therefore it is difficult to exploit efficient indexing schemes. Instead, hierarchical clustering is used to group trajectories. Moreover, the similarity measure depends heavily on two parameters, namely  $\delta$  and  $\epsilon$ . which must be known in advance, and cannot be altered dynamically without reorganization. These values determine the maximum distance between two locations of different trajectories, in time and space, respectively, to be characterized as similar. Trajectories that differ more are characterized as dissimilar and therefore their similarity is set to zero. This approach does not permit the use of ranking or incremental computation of similarity nearest-neighbor queries.

To the best of the authors' knowledge, the only research work studying trajectory similarity on networks is the work in Hwang et al. (2005, 2006). The authors propose a simple similarity measure based on POIs (points of interest). They retrieve similar trajectories on road network spaces and not in Euclidean spaces. They



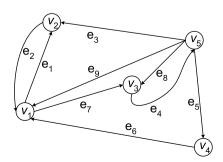


Fig. 2. A road network and its graph representation.

propose a filtering method based on spatial similarity and refining similar trajectories based on temporal distance. In order to determine the spatial similarity between trajectories, they define that two trajectories are similar in space by a set of pre-defined points of interest P if all points of P lie in both trajectories, otherwise they define the two trajectories as dissimilar. There are several drawbacks using this approach:

- The set of points of interest must be pre-defined and controlled by the user which is very restrictive.
- A simple wrong point selection in P can harm trajectory spatial similarity and the derived similarity clusters, so points in P must be selected very carefully and by an expert of the used road network.
- The similarity in space with such definition (1 = similar, 0 = dissimilar) does not take into account any notion of similarity percentage or similarity range. Therefore, we cannot determine how similar two trajectories are in space.
- The spatial similarity of two trajectories is based only into the fact that they share common points, and not into the general network space. Therefore, many similarities excluded. For example, trajectories that have parallel edges with only a city block distance and no common points, are considered completely dissimilar.

In addition, no details are given with respect to the access methods required to provide efficient similarity search. Moreover, no discussion is performed regarding the metric space properties of the proposed distance measures. Our approach avoids all these drawbacks.

In the sequel, we study in detail the proposed similarity model for trajectory similarity search in spatial networks aiming at: (i) the definition of similarity and distance measures between trajectories that satisfy the metric space properties, (ii) the exploitation of the distance between two graph nodes, which is used as a building block for the definition of trajectory similarity, (iii) the incorporation of time information in the similarity metric, and (iv) the efficient support of similarity queries by exploiting appropriate indexing schemes and applying fast processing algorithms.

# 3. Trajectory similarity measures

Let  $\mathcal{T}$  be a set of trajectories in a spatial network, which is represented by a graph G(V, E), where V is the set of nodes and E the set of edges. Each trajectory  $T \in \mathcal{T}$  is defined as:

**Table 1**Basic notations used throughout the study.

Symbol	Description	
$\mathcal{T}$	Set of trajectories	
S	Set of sub-trajectories	
$T$ , $T_a$ , $T_b$	Trajectories	
$T_q$	A query trajectory	
m	Trajectory description length	
G(V, E)	Graph representation of the spatial network	
$D_G$	Graph diameter	
$DE_G$	Maximum Euclidean node distance	
$v_i$	A node in the graph representation	
$t_i$	Time instance that the object reached node $v_i$	
e	An edge of the graph	
$T[i]. \nu$	The ith node of the trajectory	
T[i].t	The time instance that the object reached the ith node	
$d(v_i, v_j)$	Network-based distance between two nodes	
$de(v_i, v_j)$	Euclidean distance between two nodes	
$D_{netX}(T_a, T_b)$	Network-based distance between trajectories	
$D_{time}(T_a, T_b)$	Time-based distance between trajectories	
Enet	Query radius for network-based similarity	
E <sub>time</sub>	Query radius for time-based similarity	

$$T = ((\nu_1, t_1), (\nu_2, t_2), \dots, (\nu_m, t_m))$$
(1)

where m is the trajectory description length,  $v_i$  denotes a node in the graph representation of the spatial network, and  $t_i$  is the time instance (expressed in time units, e.g., seconds) that the moving object reached node  $v_i$ , and  $t_1 < t_i < t_m$ ,  $\forall 1 < i < m$ . It is assumed that moving from a node to another comes at a non-zero cost, since at least a small amount of time will be required for the transition. Table 1 gives the most important symbols and the corresponding definitions that are used in our study.

#### 3.1. Expressing trajectory similarity

We will follow a step-by-step construction of the similarity measure by first expressing similarity taking into account only the visited path, ignoring time information. Time information will be considered in a subsequent step.

We begin our exploration by assuming that any two trajectories have the same description length. This assumption will be relaxed later. Let  $T_a$  and  $T_b$  be two trajectories, each of description length m. By using our trajectory definition and ignoring the time information, we have:  $T_a = (v_{a1}, v_{a2}, \dots, v_{am})$  and  $T_b = (v_{b1}, v_{b2}, \dots, v_{bm})$ , where  $\forall i, v_{ai} \in V$  and  $v_{bi} \in V$ .

Note that, to characterize two trajectories as *similar* it is not necessary that they share common nodes. Therefore, the similarity measure must take into account the *proximity* of the trajectories (how close is one trajectory with respect to the other).

Due to motion restrictions posed by the spatial network, measuring trajectory proximity by means of the Euclidean distance is not appropriate. Instead, it is more natural to use the cost associated with each transition from a graph node to another. For example, in Fig. 4 we observe that two trajectory parts can be similar regarding the Euclidean distance, but may be dissimilar regarding the shortest path distance (network distance). Thus, for every pair of points between these two trajectory parts, the Euclidean distance is small, but the corresponding network distance is large because the long edges must be crossed. Therefore, it is important in network applications to use the network distance metric instead of the Euclidean metric.

Let  $c(v_i, v_j)$  denote the cost function to travel from a source node  $v_i$  to a destination node  $v_j$ . As we have already mentioned, this cost for the most network-based applications is defined as the shortest path distance (network distance) between the two nodes. In this paper we fix this cost to be the network distance. We also fix the following requirements for the graph representation of the network G: G must be a directed or non-directed, positive

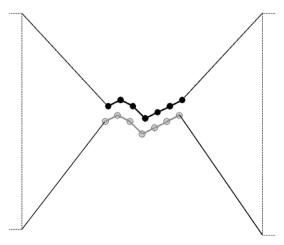


Fig. 4. Trajectory proximity.

weighted and strongly connected graph. These cases represent successfully the most real network applications (road networks, etc.).

The cost function (network distance) satisfies the following properties:

**Property I.** The cost function  $c(v_i, v_j)$  gives zero values if and only if  $v_i \equiv v_i$ .

It is obvious that c(v,v)=0 for any node v in the graph representation. It also holds that  $c(v_i,v_j)=0 \Rightarrow v_i \equiv v_j$ , because it has been assumed that any transition between nodes comes at a non-zero cost (positive weighted graphs).

**Property II.** The cost function  $c(v_i, v_j)$ , definitely satisfies the positivity property and the triangular inequality:

- $c(v_i, v_i) \geqslant 0$ ;
- $c(v_i, v_j) \leqslant c(v_i, v_x) + c(v_x, v_j)$ .

**Property III.** The cost function  $c(v_i, v_j)$ , does not satisfy in general the symmetric property, therefore it is not definitely a metric function:

•  $c(v_i, v_i) \neq c(v_i, v_i)$ .

But how does this reflect reality? Consider a directed road network with many one-way road segments, which is quite common. Then, it is clear that if a car goes from a source node  $v_i$  to a destination node  $v_j$ , it will cover a distance generally different than its way back from  $v_j$  to  $v_i$ , as it has to pass through different nodes with different weights.

# 3.1.1. Network distance measure 1

The first network distance measure  $D_{net1}$  that we propose uses network-based computations. The distance  $d(v_i, v_j)$  between any two nodes  $v_i$  and  $v_j$ , belonging to trajectories  $T_a$  and  $T_b$ , respectively, is given by the following definition.

**Definition 1.** The distance  $d(v_i, v_j)$  between two graph nodes  $v_i$  and  $v_i$  is defined as follows:

$$d(v_i, v_j) = \begin{cases} 0, & \text{if } v_i = v_j, \\ \frac{c(v_i, v_j) + c(v_j, v_i)}{2D_G}, & \text{otherwise,} \end{cases}$$
(2)

where  $D_G = \max\{c(v_i, v_j), \forall v_i, v_j \in V(G)\}$  is the diameter of the graph G of the spatial network and is a global constant for the applications. Its value can be computed taking the overall maximum of possible values of the cost function.

**Proposition 1.** The distance function  $d(v_i, v_j)$  assumes values in the interval [0, 1].

**Proof.** This is obvious when the function returns a zero value. Otherwise it returns the ratio  $\frac{c(v_i,v_j)+c(v_j,v_i)}{2D_G}$ . But, clearly we have:  $c(v_i,v_j)\leqslant D_G$  and  $c(v_j,v_i)\leqslant D_G$ , and by summation we get:  $c(v_i,v_j)+c(v_j,v_i)\leqslant 2D_G$ . Therefore, by division we get:  $d(v_i,v_j)=\frac{c(v_i,v_j)+c(v_j,v_i)}{2D_G}\leqslant 1$ . In addition, we have always  $c(v_i,v_j)\geqslant 0$  and  $c(v_j,v_i)\geqslant 0$  (positivity), thus  $d(v_i,v_j)\geqslant 0$ .  $\square$ 

**Proposition 2.** The distance function  $d(v_i, v_j)$  satisfies the metric properties.

**Proof.** We need to prove the following properties for every graph nodes  $v_i$ ,  $v_i$ ,  $v_i$ :

- (i)  $d(v_i, v_i) \ge 0$ ;
- (ii)  $d(\nu_i, \nu_j) = d(\nu_j, \nu_i)$ ;
- (iii)  $d(v_i, v_j) \leq d(v_i, v_x) + d(v_x, v_j)$ .

Clearly, property (i) is true by Proposition 1. Property (ii) is always true if  $v_i = v_j$ . Otherwise, if  $v_i \neq v_j$ , we have:

$$d(v_i, v_j) = \frac{c(v_i, v_j) + c(v_j, v_i)}{2D_G} = \frac{c(v_j, v_i) + c(v_i, v_j)}{2D_G} = d(v_j, v_i)$$

Thus, it is true in any case.

Property (iii) is obvious if  $v_i = v_j$  or  $v_i = v_x$  or  $v_j = v_x$ . Otherwise, if  $v_i \neq v_i \neq v_x$  by substitution we get:

$$\frac{c(v_i, v_j) + c(v_j, v_i)}{2D_G} \leqslant \frac{c(v_i, v_x) + c(v_x, v_i)}{2D_G} + \frac{c(v_x, v_j) + c(v_j, v_x)}{2D_G}$$
 (3)

Due to the fact that the cost function satisfies the triangular inequality, we have:

$$c(v_i, v_j) \leqslant c(v_i, v_x) + c(v_x, v_j)$$
  
$$c(v_i, v_i) \leqslant c(v_i, v_x) + c(v_x, v_i)$$

By summation and by division with  $2D_G$  we take inequality (3), thus property (iii) has been proven.  $\Box$ 

**Definition 2.** The network distance  $D_{net1}(T_a, T_b)$  between two trajectories  $T_a$  and  $T_b$  of description length m is defined as follows:

$$D_{net1}(T_a, T_b) = \frac{1}{m} \sum_{i=1}^{m} (d(v_{ai}, v_{bi}))$$
 (4)

**Proposition 3.** The distance measure  $D_{net1}(T_a, T_b)$  assumes values in the interval [0, 1].

**Proof.** Omitted.

**Proposition 4.** The distance measure  $D_{net1}(T_a, T_b)$  satisfy the metric properties.

**Proof.** We need to prove the following properties for every trajectories  $T_a$ ,  $T_b$ ,  $T_x$  of description length m:

- (i)  $D_{net1}(T_a, T_b) \ge 0$ ;
- (ii)  $D_{net1}(T_a, T_b) = D_{net1}(T_b, T_a);$
- (iii)  $D_{net1}(T_a, T_b) \leqslant D_{net1}(T_a, T_x) + D_{net1}(T_x, T_b)$ .

Clearly, property (i) is true by consulting Proposition 3. Property (ii) is true because is also true for the distance function d (Proposition 2), so:

$$D_{net}(T_a, T_b) = \frac{1}{m} \sum_{i=1}^{m} (d(v_{ai}, v_{bi})) = \frac{1}{m} \sum_{i=1}^{m} (d(v_{bi}, v_{ai})) = D_{net}(T_b, T_a)$$

Property (iii) is written equally by substitution:

$$\frac{1}{m} \sum_{i=1}^{m} (d(v_{ai}, v_{bi})) \leqslant \frac{1}{m} \sum_{i=1}^{m} (d(v_{ai}, v_{xi})) + \frac{1}{m} \sum_{i=1}^{m} (d(v_{xi}, v_{bi}))$$

$$\iff \sum_{i=1}^{m} (d(v_{ai}, v_{bi})) \leqslant \sum_{i=1}^{m} (d(v_{ai}, v_{xi})) + \sum_{i=1}^{m} (d(v_{xi}, v_{bi}))$$
(5)

From Proposition 2, we have the following inequalities:

$$d(v_{ai}, v_{bi}) \leq d(v_{ai}, v_{xi}) + d(v_{xi}, v_{bi}) \quad \forall i \in \{1, 2, \dots, m\}$$

By summation we get (5).  $\Box$ 

Fig. 5 shows two trajectories  $T_a$ ,  $T_b$  for which we are interested to calculate their distance. Assuming that  $D_G = 100$ , we have the following calculations:

$$d(v_{ai}, v_{bi}) = \left\{ \frac{17}{200}, \frac{16}{200}, \frac{9}{200}, \frac{7}{200}, 0, \frac{5}{200}, \frac{13}{200} \right\}$$

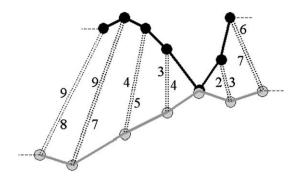


Fig. 5. Trajectory similarity example.

$$D_{net1}(T_a, T_b) = \frac{1}{7} \left( \frac{17}{200} + \frac{16}{200} + \frac{9}{200} + \frac{7}{200} + 0 + \frac{5}{200} + \frac{13}{200} \right)$$
$$= \frac{1}{7} \frac{67}{200} = 0.047857$$

#### 3.1.2. Network distance measure 2

The second distance measure,  $D_{net2}$ , that we propose uses an Euclidean-based distance function (de) in combination with the previous global constant  $D_G$  (the graph diameter by the network distance).

It can be used for fast calculations only for graphs where the coordinates of the nodes are available. In fact, in many cases the Euclidean distance results in poor performance regarding the quality of results. However, as it will be described later, it offers a "quick-and-dirty" view of the results.

**Definition 3.** The distance  $de(v_i, v_j)$  between two graph nodes  $v_i$  and  $v_i$  is defined as follows:

$$de(v_i, v_j) = \frac{euclidean(v_i, v_j)}{D_G} = \frac{\sqrt{(x_{v_i} - x_{v_j})^2 + (y_{v_i} - y_{v_j})^2}}{D_G}$$
(6)

where  $x_{v_i}$ ,  $y_{v_i}$  are the coordinates of node  $v_i$ , and  $x_{v_j}$ ,  $y_{v_j}$  are the coordinates of node  $v_j$ .

**Proposition 5.** The distance function  $de(v_i, v_j)$  assumes values in the interval [0, 1].

**Proof.** Let  $DE_G$  be the maximum Euclidean distance between all nodes of the graph representing the spatial network:  $DE_G = \max\{euclidean(v_i, v_j), \forall v_i, v_j \in V(G)\}$ . Then it is obvious that:

$$euclidean(v_i, v_i) \leq DE_G \leq D_G \quad \forall v_i, \ v_i \in V(G)$$

The last inequality holds because all network distances are always greater than or equal to the corresponding Euclidean distances. Therefore, we have:

$$\frac{\textit{euclidean}(\textit{v}_i,\textit{v}_j)}{\textit{D}_{\textit{G}}} \leqslant 1 \Longleftrightarrow \textit{de}(\textit{v}_i,\textit{v}_j) \leqslant 1$$

Moreover, as all distances are positive (or zero when  $v_i = v_j$ ), we have always:  $de(v_i, v_i) \ge 0$ .  $\Box$ 

**Proposition 6.** The distance function  $de(v_i, v_j)$  satisfies the metric properties.

**Proof.** Due to the fact that the Euclidean distance  $euclidean(v_i, v_j)$  satisfies the metric properties and  $de(v_i, v_j)$  is the Euclidean distance divided by the positive constant  $D_G$ , it is evident that  $de(v_i, v_j)$  also satisfies the metric properties.  $\square$ 

**Definition 4.** The network distance  $D_{net2}(T_a, T_b)$  between two trajectories  $T_a$  and  $T_b$  of description length m is defined as follows:

$$D_{net2}(T_a, T_b) = \frac{1}{m} \sum_{i=1}^{m} (de(v_{ai}, v_{bi}))$$
 (7)

**Proposition 7.** The distance measure  $D_{net2}(T_a, T_b)$  assumes values in the interval [0, 1].

**Proof.** Omitted.  $\square$ 

**Proposition 8.** The distance measure  $D_{net2}(T_a, T_b)$  satisfy the metric properties.

**Proof.** Omitted.

#### 3.2. Incorporating time information

The similarity measures defined in the previous section take into consideration only the traveling cost information, which depends on the spatial network. In applications such as traffic analysis, the time information associated with each trajectory is also very important.

**Definition 5.** Given two trajectories  $T_a \in \mathcal{T}$  and  $T_b \in \mathcal{T}$  of description length m, their distance with respect to time  $D_{time}(T_a, T_b)$  is given by

$$D_{time}(T_a, T_b)$$

$$=\frac{1}{m-1}\sum_{i=1}^{m-1}\frac{|(T_a[i+1].t-T_a[i].t)-(T_b[i+1].t-T_b[i].t)|}{\max\{(T_a[i+1].t-T_a[i].t),(T_b[i+1].t-T_b[i].t)\}}$$

Essentially, the time similarity between two trajectories, as it has been defined, measures their resemblance with respect to the time required to travel from one node to the next (inter-arrival times).

Fig. 6 depicts some examples for the time similarity calculations, where we have three trajectory parts  $T_a$ ,  $T_b$ ,  $T_c$  with the same description length and the inter-arrival times appear next to their directed edges.

With the previous definition we have the following calculations:

$$\begin{split} &D_{time}(T_a,T_b) = \frac{1}{4} \left( \frac{1}{5} + \frac{0}{7} + \frac{1}{4} + \frac{0}{2} \right) = 0.1125 \\ &D_{time}(T_a,T_c) = \frac{1}{4} \left( \frac{0}{5} + \frac{4}{7} + \frac{2}{6} + \frac{2}{4} \right) = 0.35119 \end{split}$$

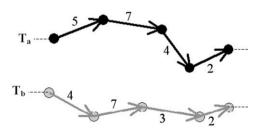




Fig. 6. Time similarity calculation example.

We observe that  $T_a$  is more similar to  $T_b$  than  $T_c$  and this happens because the corresponding inter-arrival times of the pair  $T_a$ ,  $T_b$  are much closer.

**Proposition 9.** The distance measure  $D_{time}(T_a, T_b)$  assumes values in the interval [0, 1].

**Proof.** Omitted.

**Proposition 10.** The distance measure  $D_{time}(T_a, T_b)$  satisfy the metric properties.

**Proof.** We need to prove the following properties for any trajectories  $T_a$ ,  $T_b$ ,  $T_x$  of description length m:

- (i)  $D_{time}(T_a, T_b) \geqslant 0$ ;
- (ii)  $D_{time}(T_a, T_b) = D_{time}(T_b, T_a);$
- (iii)  $D_{time}(T_a, T_b) \leq D_{time}(T_a, T_x) + D_{time}(T_x, T_b)$

Clearly, property (i) is true by Proposition 9. Let us denote the inter-arrival times of all trajectory parts of  $T_a$ ,  $T_b$  and  $T_x$  as follows:  $\delta_{ai} = T_a[i+1].t - T_a[i].t$ ,  $\delta_{bi} = T_b[i+1].t - T_b[i].t$  and  $\delta_{xi} = T_x[i+1].t - T_x[i].t$ , for all  $i=1,2,\ldots,m-1$ . Then, property (ii) is true because we have:

$$D_{time}(T_a, T_b) = \frac{1}{m-1} \sum_{i=1}^{m-1} \frac{|\delta_{ai} - \delta_{bi}|}{\max\{\delta_{ai}, \delta_{bi}\}} = \frac{1}{m-1} \sum_{i=1}^{m-1} \frac{|\delta_{bi} - \delta_{ai}|}{\max\{\delta_{bi}, \delta_{ai}\}}$$
$$= D_{time}(T_b, T_a)$$

By substitution, property (iii) is written as

$$\frac{1}{m-1} \sum_{i=1}^{m-1} \frac{|\delta_{ai} - \delta_{bi}|}{\max\{\delta_{ai}, \delta_{bi}\}} \leqslant \frac{1}{m-1} \sum_{i=1}^{m-1} \frac{|\delta_{ai} - \delta_{xi}|}{\max\{\delta_{ai}, \delta_{xi}\}} 
+ \frac{1}{m-1} \sum_{i=1}^{m-1} \frac{|\delta_{xi} - \delta_{bi}|}{\max\{\delta_{xi}, \delta_{bi}\}} \iff \sum_{i=1}^{m-1} \frac{|\delta_{ai} - \delta_{bi}|}{\max\{\delta_{ai}, \delta_{bi}\}} 
\leqslant \sum_{i=1}^{m-1} \frac{|\delta_{ai} - \delta_{xi}|}{\max\{\delta_{ai}, \delta_{xi}\}} + \sum_{i=1}^{m-1} \frac{|\delta_{xi} - \delta_{bi}|}{\max\{\delta_{xi}, \delta_{bi}\}}$$
(8)

It is sufficient to prove the following inequalities  $\forall i = 1, ..., m-1$ :

$$\frac{|\delta_{ai} - \delta_{bi}|}{\max\{\delta_{ai}, \delta_{bi}\}} \leqslant \frac{|\delta_{ai} - \delta_{xi}|}{\max\{\delta_{ai}, \delta_{xi}\}} + \frac{|\delta_{xi} - \delta_{bi}|}{\max\{\delta_{xi}, \delta_{bi}\}}$$
(9)

To prove (9) it is enough to prove that for every positive numbers *a*, *b*, *c* the following inequality holds:

$$\frac{|a-b|}{\max\{a,b\}} \leqslant \frac{|a-c|}{\max\{a,c\}} + \frac{|c-b|}{\max\{c,b\}}$$

$$\tag{10}$$

But, this inequality is obvious if a = b, or a = c, or b = c, and for all other ordering cases of the numbers a, b, c also holds:

• If *a* < *b* < *c* then it gives:

$$\frac{b-a}{b} \leqslant \frac{c-a}{c} + \frac{c-b}{c}$$

$$\iff c(b-a) \leqslant b(c-a) + b(c-b)$$

$$\iff (b+a)(c-b) \geqslant 0$$

which it holds as a, b are positive and b < c.

• If *a* < *c* < *b* then it gives:

$$\frac{b-a}{b} \le \frac{c-a}{c} + \frac{b-c}{b}$$

$$\iff c(b-a) \le b(c-a) + c(b-c)$$

$$\iff (c-a)(b-c) \ge 0$$

which it holds as a < c and c < b.

• If b < a < c then it gives:

$$\frac{a-b}{a} \leqslant \frac{c-a}{c} + \frac{c-b}{c}$$

$$\iff c(a-b) \leqslant a(c-a) + a(c-b)$$

$$\iff (a+b)(c-a) \geqslant 0$$

which it holds as a, b are positive and a < c.

• If *b* < *c* < *a* then it gives:

$$\frac{a-b}{a} \leqslant \frac{a-c}{a} + \frac{c-b}{c}$$

$$\iff c(a-b) \leqslant c(a-c) + a(c-b)$$

$$\iff (c-b)(a-c) \geqslant 0$$

which it holds as b < c and c < a.

• If c < a < b then it gives:

$$\frac{b-a}{b} \le \frac{a-c}{a} + \frac{b-c}{b}$$

$$\iff a(b-a) \le b(a-c) + a(b-c)$$

$$\iff (a+b)(a-c) \ge 0$$

which it holds as a, b are positive and c < a.

• If c < b < a then it gives:

$$\frac{a-b}{a} \leqslant \frac{a-c}{a} + \frac{b-c}{b}$$

$$\iff b(a-b) \leqslant b(a-c) + a(b-c)$$

$$\iff (a+b)(b-c) \geqslant 0$$

which it holds as a, b are positive and c < b.

Therefore, inequality (10) is true, and property (iii) has been proven.  $\Box$ 

## 3.2.1. Spatio-temporal similarity measures and methods

We have at hand different distance measures,  $D_{net}$  and  $D_{time}$ , that can be used to compare trajectories of the same length in space and time. Several applications may require both similarity measures to extract useful knowledge.

There are three different methods in order to retrieve similar trajectories in space–time as proposed in Hwang et al. (2005): (i) searching similar trajectories with direct application of spatio-temporal distance measures, (ii) filtering trajectories based on temporal similarity and refining similar trajectories based on spatial distance, (iii) filtering trajectories based on spatial similarity and refining similar trajectories based on temporal distance.

Here we suggest the methods (i) and (iii), due to the fact that method (ii) can hardly be found in practical applications.

To implement method (i) we can combine the two distance measures  $D_{net}$  and  $D_{time}$  into a single one. For example, the two distances may be weighted with parameters  $W_{net}$  and  $W_{time}$  such that  $W_{net}+W_{time}=1$ . The total (combined) distance can then be expressed as follows:

$$D_{total}(T_a, T_b) = W_{net} \cdot D_{net}(T_a, T_b) + W_{time} \cdot D_{time}(T_a, T_b)$$

It is evident that the distance measure  $D_{total}$  satisfies the metric space properties. However, this approach poses a significant limitation, since the values of  $W_{net}$  and  $W_{time}$  must be known in advance.

Consequently we propose method (iii) using  $D_{net}$  and  $D_{time}$  separately, where the distance  $D_{net}$  making the filtering step in space and the distance  $D_{time}$  making the refinement step in time. In this way, two parameter distances are required to be posed by the query. The distance  $E_{net}$  expresses the desired similarity with respect to the  $D_{net}$  distance measure, whereas the distance  $E_{time}$  expresses the desired similarity regarding the  $D_{time}$  distance measure.

If the user wishes to focus only on the network distance, then the value of  $E_{time}$  may be set to 1. Otherwise, another value is required for  $E_{time}$ , which determines the desired similarity in the time domain. By allowing the user to control the values of  $E_{net}$  and  $E_{time}$  a significant degree of flexibility is achieved, since the "weight" of each distance can be controlled at will.

#### 4. Indexing and query processing issues

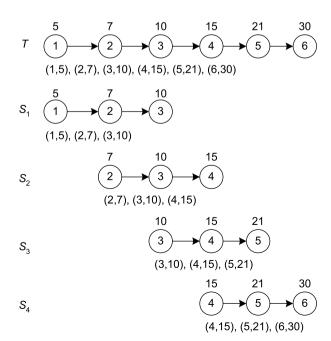
In this section, we study some important issues regarding trajectory similarity. Firstly, we discuss the problem of handling trajectories of different description length, by decomposing a trajectory to sub-trajectories. Then, we study the use of indexing schemes for sub-trajectories. Finally, we study some fundamental query processing issues.

#### 4.1. Trajectory decomposition

Up to now we have handled the case where all trajectories are of the same description length. We proceed now to relax this assumption, by considering trajectories of different lengths. In fact, this is the more general case that reflects reality. First of all, two trajectories may involve a different number of visited nodes, and therefore their description length will be different. Furthermore, we cannot always guarantee that moving objects report their positions at fixed time intervals. Due to noise, several measurements may be lost, or different moving objects report their positions at different time intervals. In these cases, two trajectories may have different description lengths.

Let T be a trajectory of description length m. Moreover, let  $\mu$  denote an integer such that  $\mu \leq m$ . T is decomposed into  $m-\mu+1$  sub-trajectories, by using a window of length  $\mu$ , and progressively moving one node at a time from left to right. Each of the resulting sub-trajectories has a length of  $\mu$ . Fig. 7 illustrates an example of the decomposition process, where m=6 and  $\mu=3$ .

By following the same process for all trajectories  $T \in \mathcal{T}$  we get a new set of sub-trajectories  $\mathcal{S}$ , all of description length  $\mu$ . Moreover, we have already defined a distance measure for trajectories of the



**Fig. 7.** Trajectory decomposition example for m = 6 and  $\mu = 3$ .

same description length in the previous section given by either  $D_{net}$  or  $D_{time}$  which both satisfy the metric space properties.

#### 4.2. Indexing schemes

Our next step involves indexing the set S of sub-trajectories, enabling efficient query processing. Towards this direction, we propose two schemes, which are both based on the M-tree access method (Ciaccia et al., 1997). Note that since a vector representation of each sub-trajectory is not available, techniques like R-trees (Guttman, 1984) and its variants are not applicable. Recall that, the M-tree is already equipped by the necessary tools to handle range and nearest-neighbor queries, as it has been reported in Ciaccia et al. (1997). The only requirement for the M-tree to work properly is that the distance used must satisfy the metric space properties. Since both  $D_{net}$  and  $D_{time}$  satisfy these properties, they can be used as distance measures in M-trees. Note that, among the metric indexing schemes we choose the M-tree because of its simplicity. However, other secondary memory schemes for metric spaces or any other metric access method can been applied equally well (e.g., SlimTrees; Traina et al., 2000). Two alternatives are followed towards indexing sub-trajectories:

- M-treel method. In this scheme, only the NET-M-tree is used to check the constraint regarding  $E_{net}$ . Then, in a subsequent step the candidate sub-trajectories are checked against the time constraints. This way, only one M-tree is used.
- M-treell method. In this scheme, two M-trees are used to handle  $D_{net}$  and  $D_{time}$  separately. These trees are termed NET-M-tree and TIME-M-tree, respectively. Each M-tree is searched separately using  $E_{net}$  and  $E_{time}$ , respectively. Then, the intersection of both results is determined to get the sub-trajectories that satisfy the network and time constraints.

#### 4.3. Query processing fundamentals

A user query is defined by a triplet  $\langle T_q, E_{net}, E_{time} \rangle$  where  $T_q$  is the query trajectory,  $E_{net}$  is the radius for the network distance and  $E_{time}$  is the radius for the time distance. For the query processing to be consistent with the proposed framework, each query trajectory  $T_q$  must be of at least description length  $\mu$ . If this is not true, padding is performed by repeating, for example, the last node of the trajectory several times, until the description length  $\mu$  is reached. In the general case where the description length of  $T_q$  is greater than  $\mu$ , the decomposition process is applied to obtain the sub-trajectories of  $T_q$ . Finally, if the description length of  $T_q$  is equal to  $\mu$ , then only one sub-trajectory is produced.

Let p denote the number of sub-trajectories of  $T_q$  determined by the trajectory decomposition process. The next step depends on the indexing scheme we utilize, i.e. either M-treel or M-treell as they have been described previously. A trajectory is part of the answer if there is at least one of its sub-trajectories that satisfy the network and time constraints for at least one query sub-trajectory. In the sequel, we analyze the whole process in detail:

- Having a query trajectory  $T_q$  of description length l and the  $E_{net}$ ,  $E_{time}$  parameters, we decompose  $T_q$  into  $p = l \mu + 1$  sub-trajectories (if  $l > \mu$ ) with the window method and then we construct their set  $QS(T_q)$ .
- For every query sub-trajectory  $qs \in QS(T_q)$ , we execute a simple range query to NET-M-Tree with radius  $E_{net}$  and collect related sub-trajectories into the set  $C_{net}$ .
- If M-treell method is used then we execute another simple range query to TIME-M-Tree with radius E<sub>time</sub> and collect related subtrajectories into the set C<sub>time</sub>.

- If M-treel method is used then we check every sub-trajectory in  $C_{net}$  against  $E_{time}$  and from the selected results we construct the set AS. Otherwise, If M-treell method is used, the results' set AS is constructed with the common sub-trajectories of the sets  $C_{net}$  and  $C_{time}$ . In both cases, the set AS contains the resulted sub-trajectories ID's.
- From the set AS we take the corresponding trajectories ID's and we construct the final result set AT.

In any case, a trajectory  $T \in \mathcal{T}$  will appear in the result set, if and only if there exists at least one sub-trajectory ts of ts which is similar to at least one sub-trajectory ts of the query trajectory ts, and also satisfies the network and time constraints. More formally:

```
T is similar to T_q \iff \exists ts \subseteq T, \exists qs \subseteq T_q : D_{net}(ts, qs) \le E_{net} \land D_{time}(ts, qs) \le E_{time}
```

Fig. 8 presents an outline of the algorithm. Taking into account that the consecutive sub-trajectories of  $T_q$  have  $(\mu-1)$  common nodes, most calculations and requests can be already in the memory, as we check one sub-trajectory after another, so it is strongly recommended to use an LRU memory buffer.

#### 4.4. Distance buffering

The distance measure  $D_{net1}$  uses the shortest path distance between graph nodes. These computations can be performed more efficiently by using an LRU buffer. The LRU buffer maintains a constant amount of distance values into main memory. In the experimental results section we show that only a relatively small buffer size is adequate to accelerate performance, offering a good hit ratio.

If the network graph has at most a few thousand nodes, it is suggested to precompute all distances  $c(v_i,v_j)$  between nodes and to put them into a hash-based file. Then, the LRU memory buffer can cooperate with this file during the request procedure for even better performance. Later, we discuss the alternative of storing only a subset of precomputed distances on the disk, to handle large graphs.

The algorithm in Fig. 9 illustrates the process of retrieving a distance  $c(v_i, v_j)$ . The variables *requests*, *hits*, and *misses* are used to test buffer performance.

It is important to remind that the LRU memory buffer and the precomputed distances disk file, are used only with  $D_{net1}$ . They are not necessary for  $D_{time}$  calculations and in  $D_{net2}$  measure which does not use network distances at all.

# 4.5. Combining measures $D_{net1}$ and $D_{net2}$ (filtering and refinement)

Due to network restrictions, a similarity range query using the  $D_{net2}$  distance measure may return some trajectories that are not similar regarding distance measure  $D_{net1}$  (false alarms). This effect is more significant when the shortest path distance between nodes is considerably higher than their Euclidean distance. Therefore, we need to detect these trajectories using another measure, which respects the network restrictions in space, and use it in a refinement step during query processing. For this reason, we can select the distance measure  $D_{net1}$  to handle false alarm detection. This procedure will give correct results if and only if we prove that every trajectory that appears in the result set of  $D_{net1}$  measure, appears also in the result set of  $D_{net2}$ , when we apply an  $E_{net}$  range query.

**Proposition 11.** For every two trajectories  $T_a$ ,  $T_b$  the following inequality always holds:

```
Algorithm SimilaritySearch(T_q, E_{net}, E_{time}, \mu)
Input
T_q: query trajectory
E_{net}: network distance radius
E_{time}: time distance radius
\mu: minimum description length of query sub-trajectory
Output
AS: set of sub-trajectory IDs
AT: set of trajectory IDs
1. QS(T_q) = all sub-trajectories of T_q of description length \mu
2. for each query sub-trajectory qs \in QS(T_q)
3.
         if method M-treeI is used then
              search NET-M-tree using qs and E_{net}
4.
5.
              C_{net} = \text{candidate sub-trajectories from NET-M-tree}
              check every sub-trajectory in C_{net} against E_{time}
6.
7.
              update AS
         else if method M-treeII is used then
8.
9.
              search NET-M-tree using qs and E_{net}
10.
               C_{net} = \text{candidate sub-trajectories from NET-M-tree}
11.
               search TIME-M-tree using qs and E_{time}
               C_{time} = \text{candidate sub-trajectories from TIME-M-tree}
12.
               AS = C_{net} \cap C_{time}
13.
14
          end if
15. end for
16. calculate AT from AS
17. \mathbf{return}(AS,AT)
```

Fig. 8. Outline of similarity search algorithm.

```
Algorithm RetrieveDistance(v_i, v_i)
Input
v_i: source node
v_i: destination node
Output
c(v_i, v_i): value of the cost function between nodes v_i and v_i
1. requests++
2. search in LRU memory buffer for distance c(v_i, v_i)
3. if distance found in buffer then
         return(c(v_i, v_j))
5.
         hits++
6. else
7.
         if a precomputed distances disk file is used then
8.
              open disk file
9.
              find record with distance c(v_i, v_i)
10.
               return(c(v_i, v_i))
11.
               insert distance c(v_i, v_j) in memory buffer with LRU rule
12.
               misses++
13.
          else
14.
               compute the distance c(v_i, v_i)
15.
               \mathbf{return}(c(v_i, v_i))
16.
               insert distance c(v_i, v_i) in memory buffer with LRU rule
17.
               misses++
          end if
18
19. end if
```

Fig. 9. Outline of distance retrieval algorithm.

$$D_{net2}(T_a, T_b) \leqslant D_{net1}(T_a, T_b)$$

**Proof.** As the shortest path distance  $c(v_i, v_j)$  between two graph nodes  $v_i$ ,  $v_j$  is always greater than or equal to their corresponding Euclidean distance, it always holds that:

$$euclidean(v_i, v_j) \leqslant c(v_i, v_j) \quad \forall v_i, \ v_j \in V$$

By dividing with the constant  $D_G$  we get:

$$\frac{\textit{euclidean}(\textit{v}_i,\textit{v}_j)}{\textit{D}_\textit{G}} \leqslant \frac{\textit{c}(\textit{v}_i,\textit{v}_j)}{\textit{D}_\textit{G}} \iff \textit{de}(\textit{v}_i,\textit{v}_j) \leqslant \textit{d}(\textit{v}_i,\textit{v}_j) \quad \forall \textit{v}_i, \ \textit{v}_j \in \textit{V}$$

Therefore, for every two trajectories  $T_a = (v_{a1}, v_{a2}, \dots, v_{am})$  and  $T_b = (v_{b1}, v_{b2}, \dots, v_{bm})$ , where  $v_{ai} \in V$  and  $v_{bi} \in V$   $(\forall i = 1, \dots, m)$ , we have the following inequalities:

$$de(v_{ai}, v_{bi}) \leqslant d(v_{ai}, v_{bi}) \quad \forall i = 1, \dots, m$$

By summation, we get:

$$\begin{split} \sum_{i=1}^{m}(de(\textit{v}_{\textit{ai}},\textit{v}_{\textit{bi}})) \leqslant \sum_{i=1}^{m}(d(\textit{v}_{\textit{ai}},\textit{v}_{\textit{bi}})) &\iff \frac{1}{m}\sum_{i=1}^{m}(de(\textit{v}_{\textit{ai}},\textit{v}_{\textit{bi}})) \\ \leqslant \frac{1}{m}\sum_{i=1}^{m}(d(\textit{v}_{\textit{ai}},\textit{v}_{\textit{bi}})) &\iff \textit{D}_{\textit{net2}}(\textit{T}_{\textit{a}},\textit{T}_{\textit{b}}) \leqslant \textit{D}_{\textit{net1}}(\textit{T}_{\textit{a}},\textit{T}_{\textit{b}}) \end{split}$$

and the proposition has been proven.  $\ \ \Box$ 

Following Proposition 11, when we have a query trajectory  $T_q$  and a network query range  $E_{net}$ , all trajectories returned by  $D_{net1}$  measure will appear in the result set of  $D_{net2}$ , because:

$$D_{net2}(T_q,T) \leqslant D_{net1}(T_q,T) \leqslant E_{net} \quad \forall T \in \mathcal{T}$$

Fig. 10 illustrates the outline of the similarity search algorithm including the refinement step.  $D_{net2}$  is used as the filtering distance measure, whereas  $D_{net1}$  is used for refinement, to eliminate false

alarms. An important observation is that this scheme can be applied to both M-treel and M-treell methods, and moreover, it can be used with any well-defined distance measure, as long as the following lower-bounding property holds:

$$D_{\text{filtering}}(T_a, T_b) \leqslant D_{\text{refinement}}(T_a, T_b) \quad \forall T_a, T_b \in \mathcal{T}$$

#### 5. Performance evaluation

In this section, we give information about the implementation of the proposed approach in C++ and the results of experiments that confirm and evaluate all previous algorithms, procedures and techniques. All experiments have been conducted on a Pentium IV running Windows XP, with 1 GB of RAM, and a 320 GB-SATA2-16 MB hard disk. First, we present the construction of used spatial network and trajectory data set. Then, we present the construction of M-Trees for each defined measure and how the proposed measures express well the notion of similarity in space and time. At the main part, we present the evaluation results of all proposed methods for similarity range queries.

#### 5.1. Spatial network data

All experiments have been conducted using a real-world spatial network, the road network of Oldenburg city (Brinkhoff, 2002). The cost function  $c(v_i, v_j)$  between two nodes of the graph representation is the shortest path distance. The number of vertices in the Oldenburg data set is 6105. Therefore, the total number of precomputed distances among all possible pairs of vertices is 37,271,025. These distances are stored in a hash-based file on disk (DISTfile), using the Hilbert space filling curve as a hashing function. The Hilbert curve values are derived from the corresponding source and target node ID's of the distances, which are integers into the

```
Algorithm SimilaritySearchWithRefinement(T_a, E_{net}, E_{time}, \mu)
Input
T_q: query trajectory
E_{net}: network distance radius
E_{time}: time distance radius
\mu: minimum description length of query sub-trajectory
Output
ASF: final set of sub-trajectory IDs
ATF: final set of trajectory IDs
1. QS(T_q) = all sub-trajectories of T_q of description length \mu
2. ASF = \emptyset
3. for each query sub-trajectory qs \in QS(T_q)
      if method M-treeI is used
        search NET-M-tree (constructed by the basic metric) using qs and E_{net}
5.
6.
        C_{net} = candidate sub-trajectories from NET-M-tree (using the D_{net} distance of the basic metric)
7.
        check every sub-trajectory in C_{net} against E_{time}
8.
        update AS
9.
      else if method M-treeII is used then
10.
         search NET-M-tree (constructed by the basic metric) using qs and E_{net}
11.
         C_{net} = \text{candidate sub-trajectories from NET-M-tree} (using the D_{net} distance of the basic metric)
12.
         search TIME-M-tree using qs and E_{time}
         C_{time} = candidate sub-trajectories from TIME-M-tree
13.
         AS = C_{net} \cap C_{time}
14.
15.
       end if
16.
       for each sub-trajectory S_i in AS
17.
         compute the D_{net} distance of S_i from qs using the selected refinement metric
18.
         insert S_i in ASF if that distance is less than or equal to E_{net}
19.
       end for
20. end for
21. calculate ATF from ASF
22. \mathbf{return}(ASF, ATF)
```

Fig. 10. Outline of similarity search algorithm with refinement step.

interval  $[0, |V_G| - 1]$ , (e.g., for the distance  $c(v_i, v_j)$  the value  $Hilbert(ID(v_i), ID(v_j))$  is calculated). For the selected road network, the total time required for all precomputations and creation of DISTfile is 3,180.581 s. The record length has been set to 16 bytes, so the final file capacity is 596,336,400 bytes (285 MB zipped).

An in-core LRU buffer has been used to keep a number of precomputed distances in main memory (we initialized the buffer selecting some top-used distances through calculations which actually are distances between nodes that included in the most trajectory parts). The size of the buffer has been set to 2000, which is a relatively small value compared to the total number of pair-wise distances. We have computed the average number of network distance calculation requests, the average number of hits and misses, in simple range queries in space using  $D_{net1}$  and  $D_{net2}$ . The results show that almost 85% of the distance requests are absorbed by the main memory buffer and therefore, we avoid fetching them from the disk. The more buffer pages are available, the higher the hit ratio becomes.

The fast retrieval of shortest path distances is the most time consuming factor affecting the performance of network-based distance calculations, the construction of M-Trees and finally in the performance of similarity range queries.

#### 5.2. Construction of trajectories and sub-trajectories

The trajectory data set  $\mathcal{T}$  we have used for the experiments consists of 3797 trajectories of objects moving on the road segments of

Oldenburg city, using the generator developed in Brinkhoff (2002). Each trajectory has a minimum description length of 10 and maximum description length of 100 nodes. A sliding window of description length  $\mu=10$  has been used to generate the sub-trajectories of each trajectory. Therefore, the total number of sub-trajectories produced (set  $\mathcal{S}$ ) is 75,144.

Moreover, it is important to study the distribution of the constructed trajectory data set among the nodes of the road network. This will help to evaluate if the data set represents well a realworld trajectory set of this town. So, we record in a new file all node ID's used by the trajectories, with the frequency that are being used (how many trajectories pass through) in a descending order. Fig. 11a gives the recorded distribution and Fig. 11b depicts the top-100 most used nodes in the network by the trajectories.

It is evident that we have a skew distribution of nodes in trajectories and this reflects reality: there are some nodes that are being used very often which are center points of this town or hard traffic points, and the most peripheral nodes are being used much rarely. Therefore, our trajectory data set is a good representative of a real traffic condition.

#### 5.3. M-tree construction

We have constructed four different M-trees. The NET-M-trees which are implemented based on the  $D_{net1,2,3}$  measures and the TIME-M-tree implemented based on the  $D_{time}$  measure. Recall that,

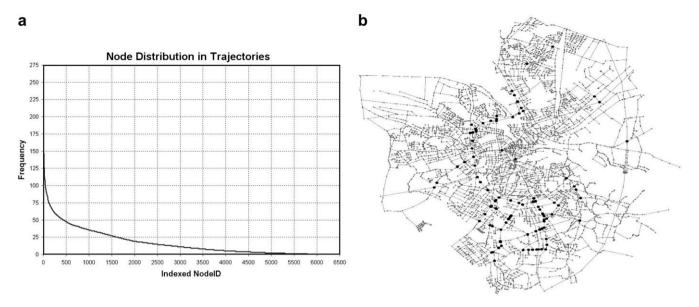


Fig. 11. (a) Distribution of nodes in trajectories; (b) top-100 most frequent nodes.

all M-trees handle the same set S of sub-trajectories of description length  $\mu = 10$  and not the complete trajectories of moving objects.

We have utilized the bulk-loading method for the construction of all M-trees, and the following parameters values have been used: a page size of 4 KB, 5% minimum node utilization, minimum overlaps promote part and root functions, a general hyper-plane split strategy, and radius function by average. Table 2 shows the total number of network distances computed during the construction, the number of zero distances, the final file capacity of M-trees on disk and the total construction time. Note that we have exploited precomputed distances (LRU buffer and DISTfile) during the construction procedure.

We observe that  $D_{net2}$  gives the smallest capacity and construction time, because network distance computations are not required.

### 5.4. Evaluation of similarity measures

We have randomly selected several trajectories from different areas of Oldenburg and we have performed similarity range queries by using all measures.

Figs. 12 and 13 show the results of range queries with radius  $E_{net} = 0.01$ , 0.05, 0.10, in a random selected query trajectory from our data set, using the available network distance measures. By studying these figures we observe that:

- In all metrics, the resulted trajectories firstly appeared in the closest neighbor of query trajectory and as the radius E<sub>net</sub> increases, they expand into connected and almost rounded areas, in which the query trajectory takes a central position.
- All query trajectory results of D<sub>net1</sub> metric (using a constant E<sub>net</sub> range) are included in the results of D<sub>net2</sub> metric, according to Proposition 11.

**Table 2** Information regarding the construction of M-trees.

M-tree	Distances	Zeros	Capacity (MB)	Time
$D_{net1}$	1,574,890	38,309	32.5	13 min + 7 s
$D_{net2}$	1,494,416	37,761	32.1	35 s
$D_{time}$	4,013,864	40,461	30.9	1 min + 46 s

#### 5.5. Performance evaluation of M-treeI and M-treeII methods

In this section, we study the performance of M-treel,II methods using all the proposed metrics. We selected randomly 100 trajectories from our data set and from different parts of the town and we performed similarity range queries using the M-treel,II methods. We gave all combination values into the interval [0,1] with a step of 0.05 in  $E_{net}$ ,  $E_{time}$  parameters. The final reported results correspond to the average values of these 100 queries. The basic parameters that are studied are summarized in Table 3.

Fig. 14a depicts the number of similar sub-trajectories found using all available network-based distance measures. Recall, that the results are the same for both M-treel and M-treelI methods. As the  $E_{net}$  radius increases,  $D_{net2}$  first reaches the upper limit (75,144), followed by  $D_{net1}$ . Evidently, the distance measure  $D_{net2}$  gives more results than  $D_{net1}$  due to the lower-bounding property.

Fig. 14b depicts the total time spent for network-based computations using all network-based distance measures. It is evident that  $D_{net2}$  is the less time consuming measure since distances are computed by using the Euclidean distance of the nodes. The results are similar for both M-treel and M-treell methods.

Fig. 15 illustrates the memory LRU buffer activity using  $D_{net1}$ . Note that  $D_{net2}$  does not use the LRU buffer, since no network distance computations are performed. In both cases, the total number of distance hits is about 85%, so with only 2000 buffer pages we have a satisfactory hit ratio. Again, the results are similar for M-treel and M-treel methods.

Fig. 16 depicts the number of time-based distance computations for M-treel and M-treelI methods. We observe that in M-tree-II method the number of time-based distance computations depends only on the  $E_{time}$  radius, whereas in M-treel method this value depends on both  $E_{net}$  and  $E_{time}$  parameters, because in this case the total number of computed distances is equal to the number of sub-trajectory results returned by the NET-M-tree. Therefore, we expect less time-based computations in the M-treel method than in the M-treelI method. This results in slightly better performance for the M-treel method regarding time-based distance computation overhead, as it is illustrated in Fig. 17.

Fig. 18 depicts the percentage of false alarms for  $D_{net2+1}$ , for various values of parameters  $E_{net}$  and  $E_{time}$ . In the left part of the figure, these parameters change freely, whereas in the right part always



Fig. 12. Preview of range queries using distance measure  $D_{net1}$ .

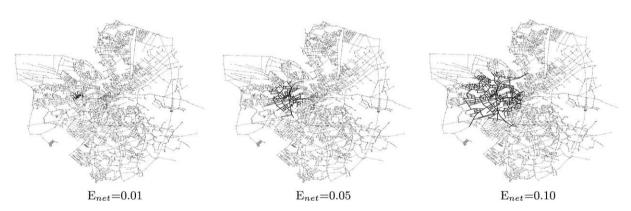


Fig. 13. Preview of range queries using distance measure  $D_{net2}$ .

**Table 3**Basic variables measured throughout experiments.

Variable	Description
N <sub>net</sub>	Number of similar sub-trajectories found in NET-M-tree
$D_{net}$	Number of network-based distance computations
$T_{net}$	Total searching time in NET-M-tree (s)
MBFR	Memory LRU buffer total requests
MBFH	Memory LRU buffer total hits
MBFM	Memory LRU buffer total misses
DBFR	Disk LRU buffer total requests
DBFH	Disk LRU buffer total hits
DBFM	Disk LRU buffer total misses
N <sub>time</sub>	Number of similar sub-trajectories found in TIME-M-tree
$D_{time}$	Number of time-based distance computations
$T_{time}$	Total searching time in TIME-M-tree (M-treeII) or in time calculations (M-treeI) (s)
TT	Total query time
AS	Total number of common (M-treell) or accepted (M-treel) sub-trajectories found (Net&Time)
AT	Total number of similar trajectories found (final results)
FA	False alarms for sub-trajectories in $D_{net2+1}$ method

 $E_{net}$  equals  $E_{time}$ . It is evident, that the existence of false alarms cannot be avoided, due to the distance lower-bounding. However, the percentage of false alarms is relatively small, and therefore effective filtering is performed by applying the Euclidean distance prior to network distance computations. The maximum number of false alarms (around 25%) appears when  $E_{net} = 0.25$  and  $E_{time} = 0.30$ .

Fig. 19a and b depict some representative results regarding the performance of M-treel and M-treell methods for  $E_{net} = E_{time}$ , using all network distance measures.  $D_{net2}$  is the most efficient tool but needs validation of correctness, and  $D_{net2+1}$  method is the most attractive alternative that can be used for trajectory similarity search, if efficiency is important. However, care should be taken since the usage of  $D_{net2+1}$  involves determination of false alarms.

If the number of false alarms is large, performance degradation may appear.

In all the experiments conducted, the method that uses only one M-tree performs marginally better than the method that utilizes two M-trees (one for  $D_{net}$  and one for  $D_{time}$ ). However, the existence of two M-trees offers a higher degree of flexibility during query processing, since we can search for similar trajectories based: (i) only on network distance  $D_{net}$ , (ii) only on time distance  $D_{time}$  and (iii) both on network and time distances  $D_{net}$  and  $D_{time}$ . Moreover, different clustering schemes can be applied. More specifically, using the two separate M-trees, a clustering algorithm can provide clusters for  $D_{net}$  or  $D_{time}$ . Finally, more choices for query optimization are available if both indexes are utilized, since the

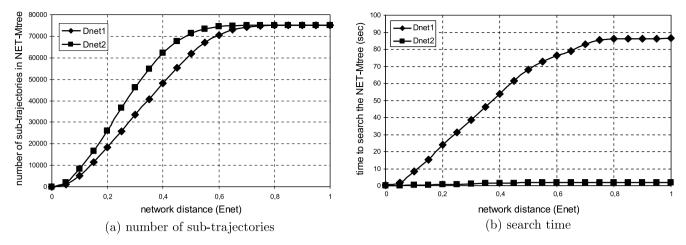
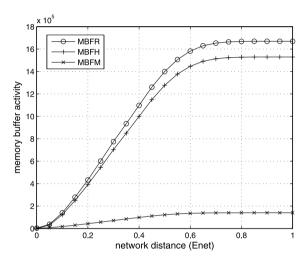


Fig. 14. Number of sub-trajectories (a) and search time (b) for NET-M-tree.



**Fig. 15.** Memory buffer activity for  $D_{net1}$ .

query execution engine can form an efficient query execution plan according to the selectivities of the search distances  $E_{net}$  and  $E_{time}$ , and traverse the M-trees accordingly.

# 5.6. Impact of precomputed distances

The previous experiments have been conducted by having all network distances precomputed and stored on disk. It has been observed that the precomputation reduces the required computational costs during network-based distance calculations. However, the precomputation assumption may not be realistic in very large spatial networks containing many thousands of nodes. However, even for small spatial networks, if the main memory buffer fails to achieve an acceptable hit ratio, many distance computations will be invoked, resulting in performance degradation.

Figs. 20 and 21 show some interesting results regarding the performance of trajectory similarity queries, when only a subset of the total distances are precomputed. The performance of  $D_{net1}$  measure is illustrated in Fig. 20, which depicts the activity of the memory-based (a) as well as the disk-based buffer (b). It is evident that by increasing the number of precomputed distances the total running time of trajectory similarity queries decreases but the cost is still significant, raising problems for ad-hoc query processing. On the other hand, the use of the Euclidean distance for filtering purposes results in a much more efficient scheme, as it is illustrated in Fig. 21.

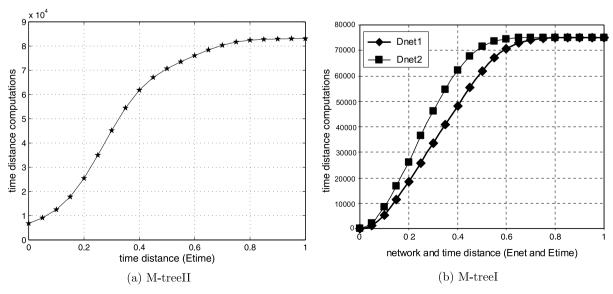


Fig. 16. Number of time-based distance computations in M-treel and M-treell methods.

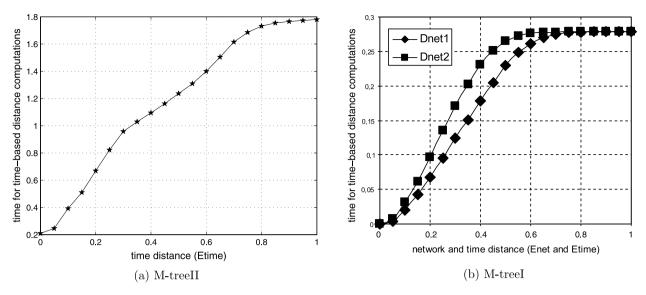
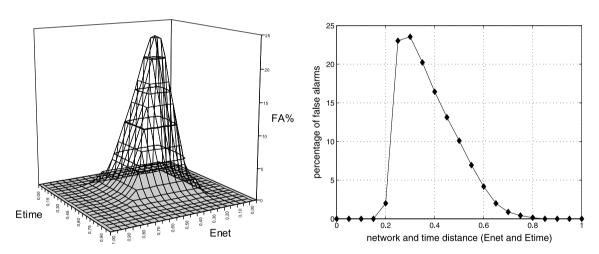


Fig. 17. CPU time (in s) required for time-based distance computations in M-treel and M-treell methods.



**Fig. 18.** Percentage of false alarms for  $D_{net2+1}$  method.

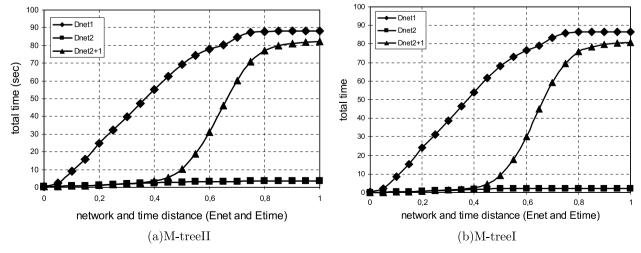


Fig. 19. Total running time (in s) for M-treell and M-treel methods.

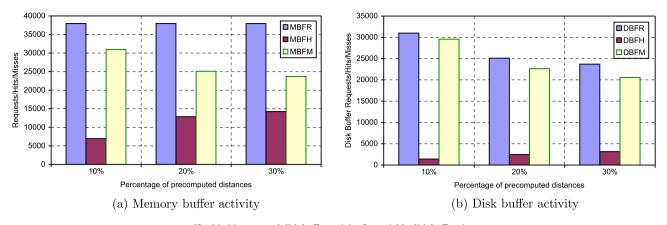
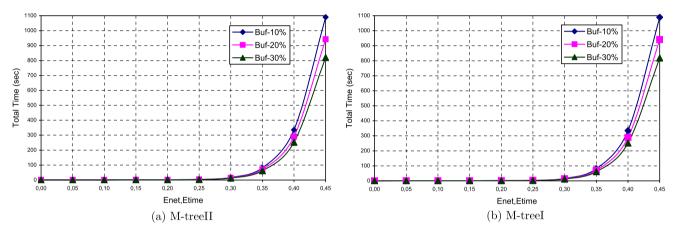


Fig. 20. Memory and disk buffer activity for variable disk buffer sizes.



**Fig. 21.** Total running time for  $D_{net2+1}$  for variable query radius and disk buffer sizes.

#### 6. Conclusions

Although there is significant research work performed on trajectory similarity on moving objects trajectories, the vast majority of the proposed approaches assume that objects can move freely without any motion restrictions. In this paper, we have studied the problem of trajectory similarity query processing in network-constrained moving objects. We have defined two concepts of similarity. The first is based on the network distance and the second is based on the time characteristics of the trajectories. By using these concepts, we have defined distance measures  $D_{net}$  to capture the network similarity and a distance measure  $D_{time}$  to capture the time-based similarity of trajectories. All proposed measures satisfy the metric space properties, and therefore, metric-based access methods can be used for efficient indexing and searching.

To support trajectories of different description lengths, a decomposition process is applied. Each trajectory is split to a number of sub-trajectories, which are then indexed by M-trees. The NET-M-tree is used for the  $D_{net}$  measure, whereas the TIME-M-tree is used for the  $D_{time}$  measure. Two methods have been studied: (i) the M-treel method, which uses only the NET-M-tree and (ii) the M-treell method, which utilizes both trees. Performance evaluation results show that trajectory similarity can be efficiently supported by these schemes. In all the experiments conducted, the method that uses only one M-tree performs marginally better than the method which utilizes two M-trees. However, the existence of two M-trees offers a higher degree of flexibility during query processing.

Future research may involve: (i) the investigation of alternative indexing schemes, (ii) the study of approximate processing, (iii) the efficient support of trajectory-based k-nearest-neighbor processing, and (iv) the utilization of the proposed similarity measures for data mining (e.g., trajectory clustering).

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